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BEST

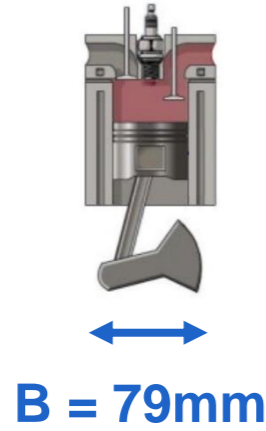
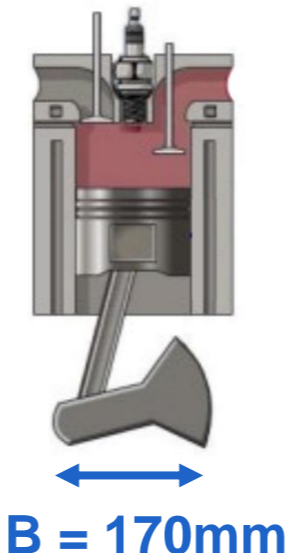

Fifth consortium meeting, 23/05/2022, Ward Suijs



THROWBACK

- Goal statement within the project:
 - Compute the efficiency potential of a **methanol fueled SI ICE**, as function of its size

Q: How to predict the performance of differently sized engines?

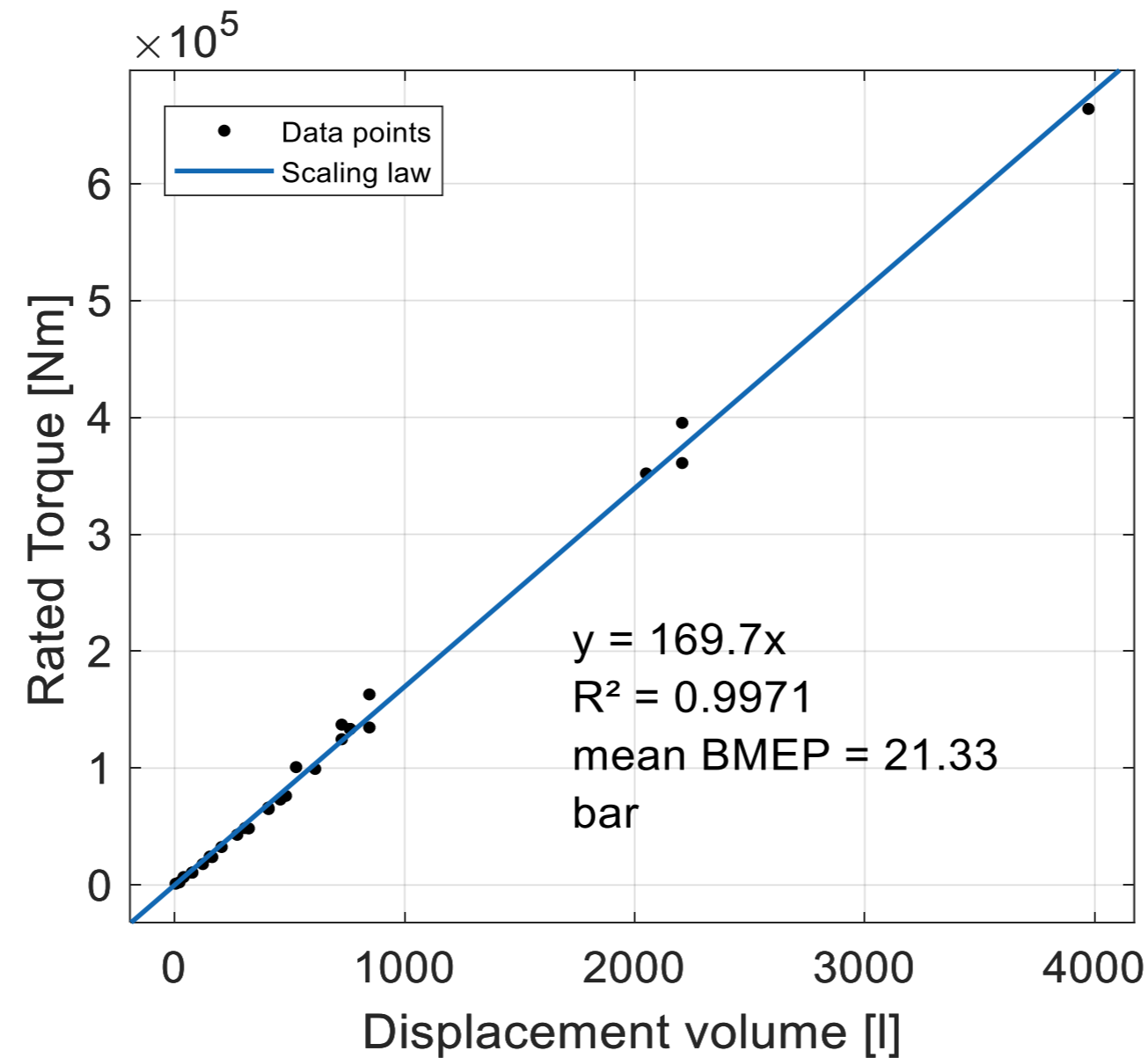
		
$V_d = 1.6l$	$V_d = 50l$	$V_d = 500l$
$\eta_{max} = 42\%$	$\eta_{max} = ?$	$\eta_{max} = ?$
@ $P = 52 kW$	@ $P = ?$	@ $P = ?$

SCALING LAWS

- Intent: predict the important operating conditions (efficiency and power) based on the size requirement of the engine
- Literature review:
 - Curve fitted scaling laws
 - Willans Line method
 - Similitude
 - Review paper submitted to SAE PFL 2022

CURVE FITTED EQUATIONS

- Constructing an empirical curve that best fits to a series of data points



CURVE FITTED EQUATIONS

- Standard form: $y = a \cdot x^b$
 - Menon et al¹.: $P [kW] = 37.919 \cdot V_d^{0.9543}$ & $BTE [\%] = 15.322 \cdot V_d^{0.0688}$
 - Brown et al².: $P [kW] = 225.05 \cdot V_d^{0.74}$
- More pragmatic approach: start from fundamental engine performance parameters:

– $BMEP [bar] = \frac{4\pi \cdot T}{V_d}$

Chon and Heywood³ → $P [kW] = \frac{N \cdot BMEP}{1200} \cdot V_d$

Heywood⁴ → $P [kW] = \frac{c_m \cdot BMEP}{400} \cdot A_p$

Heywood⁴ → $P [kW] = 0.23 \cdot BMEP \cdot c_m \cdot V_d^{\frac{2}{3}} \cdot N_c^{\frac{1}{3}}$

CURVE FITTED EQUATIONS

- More pragmatic approach: start from fundamental engine performance parameters:

- $BMEP [bar] = \frac{4\pi \cdot T}{V_d}$

- $SA/V_d [cm^{-1}] = \frac{4}{B} + \frac{2}{S}$

Rowton⁵

$$P [kW] = \frac{\rho_{pwr} \cdot \pi}{4} \cdot \left(\frac{SA/V_d}{6} \right)^{-3}$$

$$BTE [\%] = 21 \cdot \left(SA/V_d \right)^{-1.5}$$

$$BTE [\%] = 0.0125 \cdot V_d^{1.5} + 7$$

CURVE FITTED EQUATIONS: QUALITY OF FIT?

- Case study: set of 30 heavy duty SI gas engines
 - $B > 100$ mm
 - $V_d \in [5 - 4000]$ liter
 - Pre-chamber ignited



Mahle jet ignition system:

<https://www.youtube.com/watch?v=n6Eutw0WU3U>

CURVE FITTED EQUATIONS: QUALITY OF FIT?

- Case study: set of 30 heavy duty SI gas engines
 - $B > 100\text{mm}$
 - Pre-chamber ignited
 - $V_d \in [5 - 4000]$ liter
- Quality of fit: R^2

Power [kW]		BTE [%]	
Scaling law	R^2	Scaling law	R^2
Menon ¹	0.9664	Menon ¹	0.6495
Chon & Heywood ³	0.9516	Rowton ⁵	0.5168
Chon & Heywood ³	0.9813	Rowton ⁵	0.7369
Menon ¹	0.9805		
Chon & Heywood ³	0.8430		

$$P [kW] = \frac{c_m \cdot BMEP}{400} \cdot A_p$$

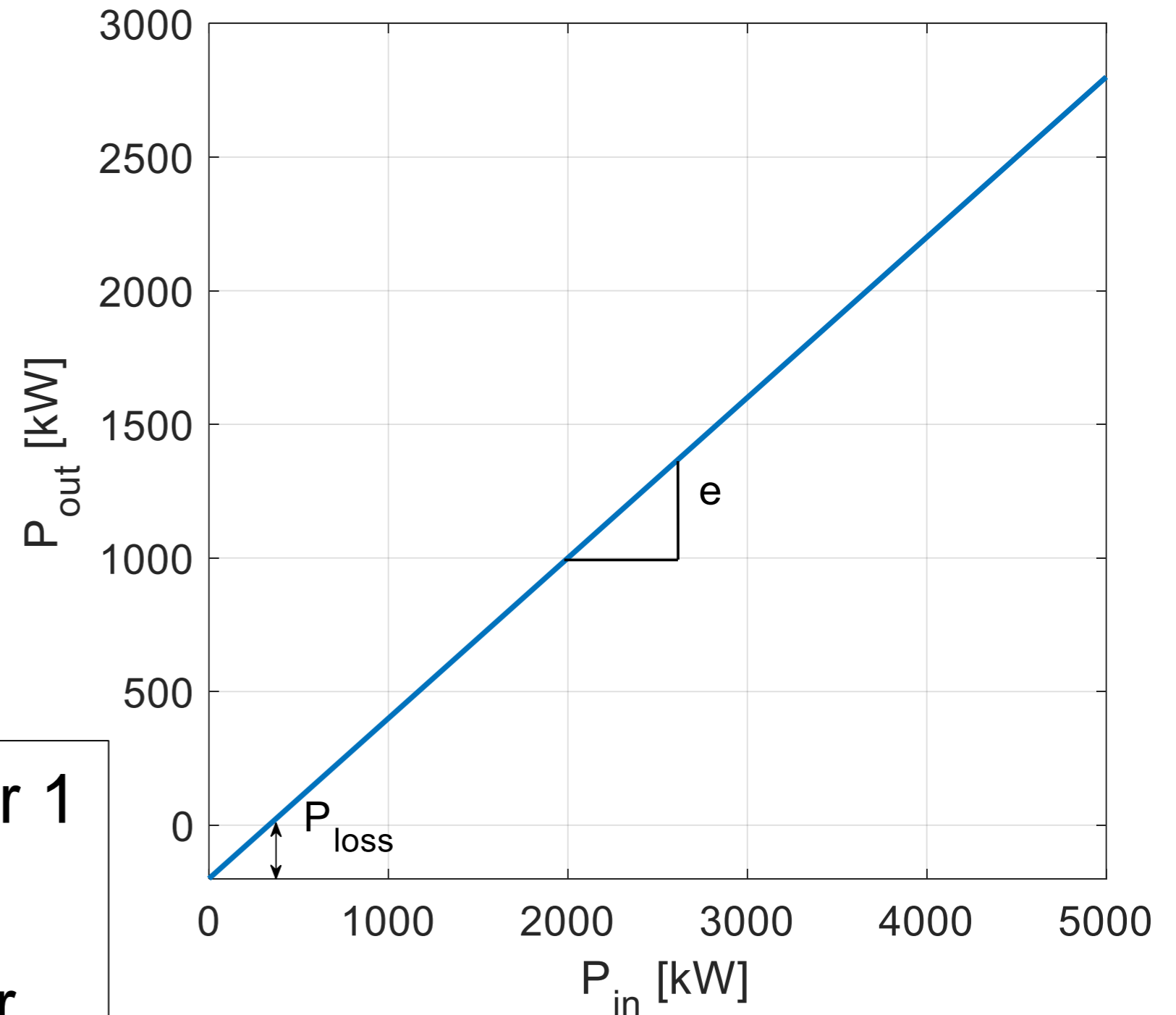
$$BTE [\%] = 0.0125 \cdot V_d^{1.5} + 7$$

WILLANS LINE METHOD

- Scaling law for fuel consumption
- Assumes that:
 - At constant N [rpm]: $bsfc \sim load$
 - $P [kW] = e \cdot P_{in} - P_{loss}$
 - Writing it independently of V_d :
 - $BMEP [Pa] = e \cdot AMEP - p_{m_{loss}}$

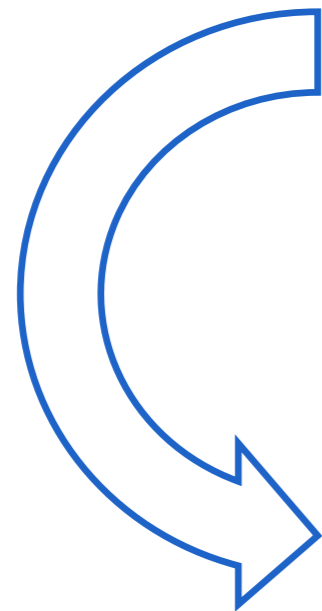
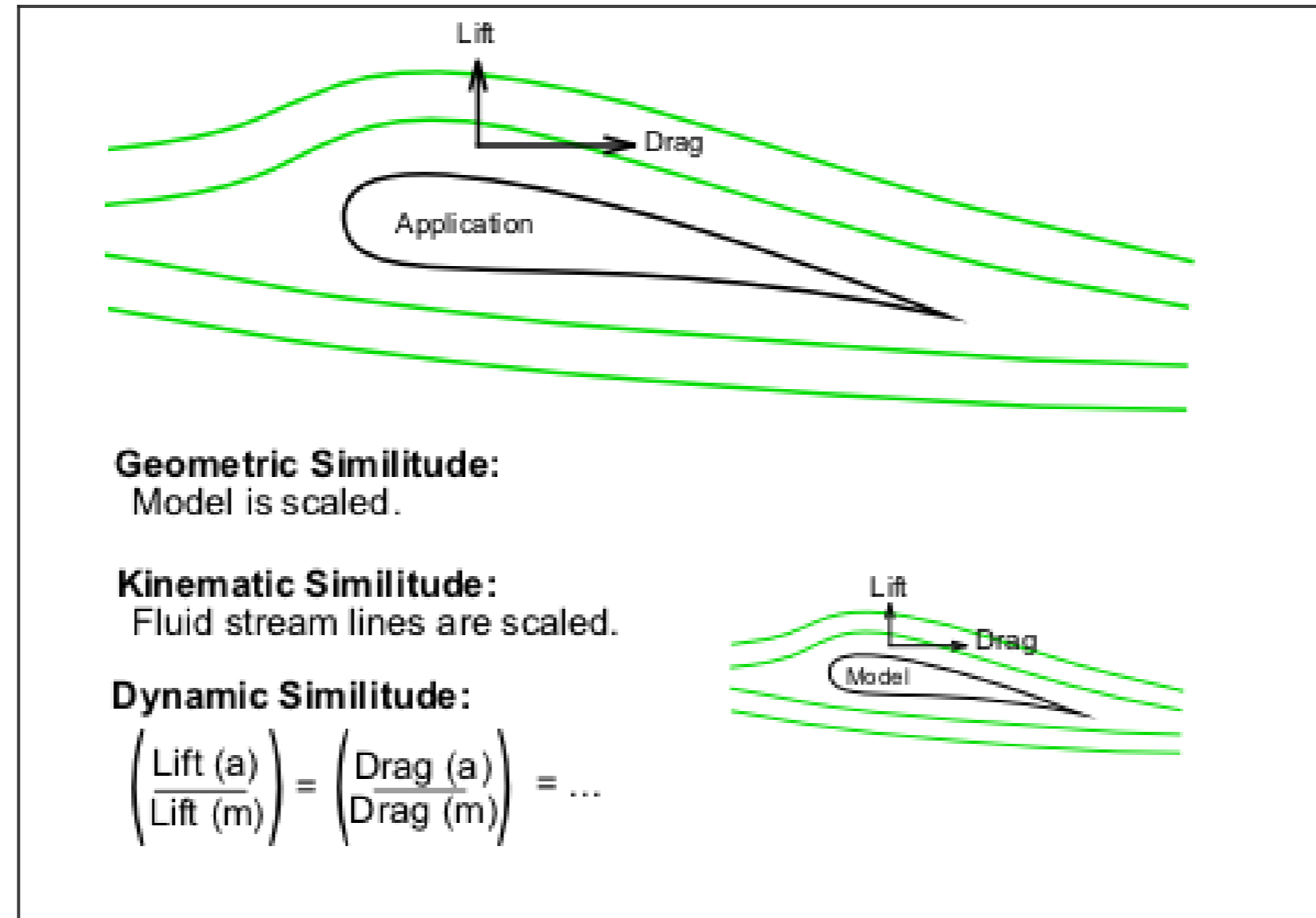
Rizzoni et al⁶.: If BMEP and AMEP known for 1 optimized engine

→ e & $p_{m_{loss}}$ can be calculated and used for other sized engines



SIMILITUDE/SIMILARITY

- Concept originating from fluid mechanics



If similarity achieved → All dimensionless performance parameters equal to each other

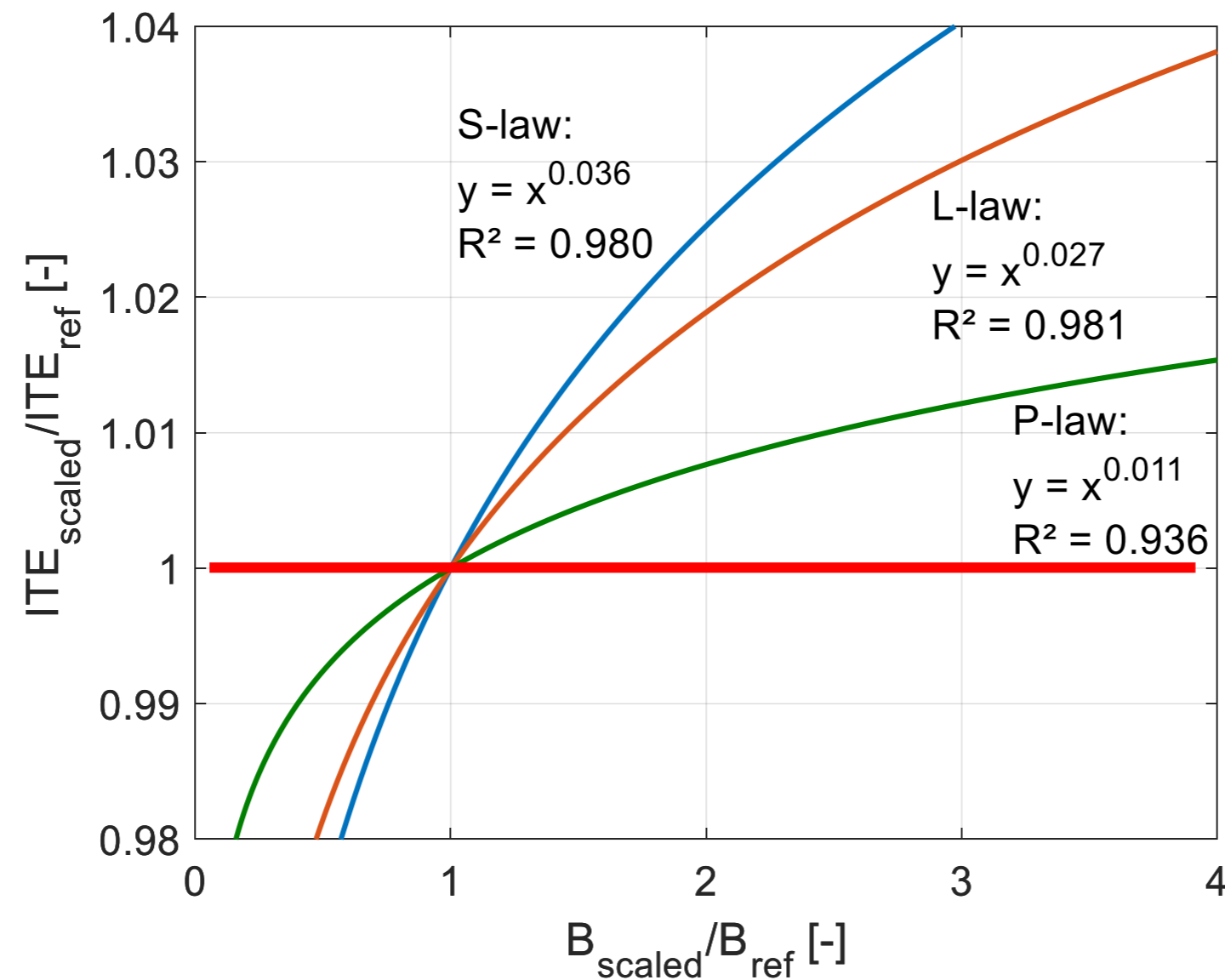
SIMILITUDE/SIMILARITY

- Applied to ICEs: If small engine and large engine achieve similarity → **BTE [%]** and **specific power [kW/l]** identical
- For CI engines, 3 different approaches were established to reach similarity: S-law, P-law and L-law

Parameters	Speed rule	Pressure rule	Lift-off rule
Bore ratio (B_{scaled}/B_{ref})	r	r	r
Lift-off length ratio (H_{scaled}/H_{ref})	$r^{4/3}$	$r^{1/3}$	r
Ratio of swirl ratio's (SR_{scaled}/SR_{ref})	1	1	1
Fuel mass flow rate ratio ($\dot{m}_{f,scaled}/\dot{m}_{f,ref}$)	r^3	r^3	r^3
Engine speed ratio (N_{scaled}/N_{ref})	1	r^{-1}	$r^{-1/3}$
Injection rate ratio ($u_{0,scaled}/u_{0,ref}$)	r	1	$r^{2/3}$
Injection duration ratio (τ_{scaled}/τ_{ref}) [s]	1	r	$r^{1/3}$
Injection pressure ratio ($\Delta P_{scaled}/\Delta P_{ref}$)	r^2	1	$r^{4/3}$

SIMILITUDE/SIMILARITY

- Theory ↔ Reality
 - Example: ≠ heat losses
- Solution:



→ e.g.: P-law: $ITE_{scaled} [\%] = 50.63 \cdot V_{d,scaled}^{0.004}$

PROS AND CONS

Curve fitted equations

- 👍 Ease of implementation
- 👍 Rapid result
- 👎 Large set of data is needed
- 👎 No boundary conditions or constraints defined
- 👎 No scaling laws with respect to emissions found

Willans line method

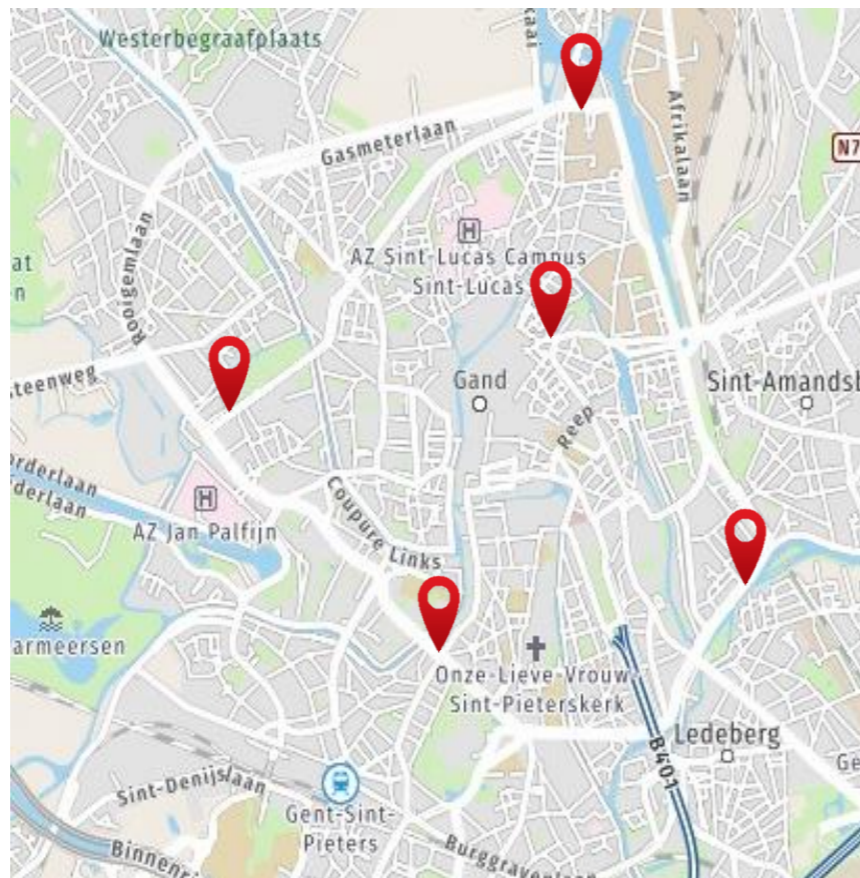
- 👍 Ease of implementation
- 👍 Rapid result
- 👍 Only 1 reference engine needed
- 👎 No boundary conditions or constraints defined
- 👎 Designed for small changes in V_d
- 👎 Limited to scaling fuel consumption

Similitude

- 👍 Already defines some design parameters
- 👍 Only 1 reference engine needed
- 👍 Constraints implemented
- 👎 Complex
- 👎 Yet unproven for SI operation

FUTURE PERSPECTIVES

- In the short term: curve fitted equations show the highest potential
 - Next requirement: gather/create as much engine data as possible
 - Example: Thesis 2022-2023: conversion of 7.15l CI diesel engine to SI methanol operation
- If we then know, both cost and the efficiency of a large range of engines, we can make the following exercise:



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